

III

Найти решение задачи Коши для системы дифференциальных уравнений методом исключения и операционным методом.

1.
$$\begin{cases} x' = x - 2y \\ y' = x - y \end{cases} \quad x(0) = 1, y(0) = 0$$

2.
$$\begin{cases} x' = x + y \\ y' = 8x + 3y \end{cases} \quad x(0) = 0, y(0) = 2$$

3.
$$\begin{cases} x' = x - 4y \\ y' = x + y \end{cases} \quad x(0) = 0, y(0) = 1$$

4.
$$\begin{cases} x' = x + y \\ y' = -x - y \end{cases} \quad x(0) = -2, y(0) = 1$$

5.
$$\begin{cases} x' = 2x - y \\ y' = x + 4y \end{cases} \quad x(0) = 1, y(0) = 0$$

6.
$$\begin{cases} x' = -x + y \\ y' = -2x + y \end{cases} \quad x(0) = 0, y(0) = 1$$

7.
$$\begin{cases} x' = 3x + y \\ y' = -x + y \end{cases} \quad x(0) = 3, y(0) = 0$$

8.
$$\begin{cases} x' = 3x + y \\ y' = -x + 5y \end{cases} \quad x(0) = 0, y(0) = 2$$

9.
$$\begin{cases} x' = 5x - y \\ y' = x + 3y \end{cases} \quad x(0) = 1, y(0) = 0$$

10.
$$\begin{cases} x' = 12x - 5y \\ y' = 5x + 12y \end{cases} \quad x(0) = 1, y(0) = 1$$

11.
$$\begin{cases} x' = x - y \\ y' = 4x - 3y \end{cases} \quad x(0) = 3, y(0) = 0$$

12.
$$\begin{cases} x' = -x - 10y \\ y' = 2x + 3y \end{cases} \quad x(0) = 7, y(0) = -1$$

13.
$$\begin{cases} x' = 3x - y \\ y' = x + 5y \end{cases} \quad x(0) = 2, y(0) = 1$$

14.
$$\begin{cases} x' = -2x - 5y \\ y' = x \end{cases} \quad x(0) = 7, y(0) = -1$$

15.
$$\begin{cases} x' = x - 2y \\ y' = 2x - 3y \end{cases} \quad x(0) = 0, y(0) = 1$$

16.
$$\begin{cases} x' = x + y \\ y' = -4x + y \end{cases} \quad x(0) = 1, y(0) = 2$$

17.
$$\begin{cases} x' = -3x + 4y \\ y' = -x + y \end{cases} \quad x(0) = 0, y(0) = 3$$

18.
$$\begin{cases} x' = 4x + 15y \\ y' = -3x - 2y \end{cases} \quad x(0) = 7, y(0) = -1$$

19.
$$\begin{cases} x' = -3x + 2y \\ y' = -2x + y \end{cases} \quad x(0) = 1, y(0) = 0$$

20.
$$\begin{cases} x' = 3x - y \\ y' = x + y \end{cases} \quad x(0) = 1, y(0) = 2$$

21.
$$\begin{cases} x' = 12x + 5y \\ y' = -5x + 12y \end{cases}$$

22.
$$\begin{cases} x' = 5x + 4y \\ y' = -x + y \end{cases}$$

$$x(0) = 2, y(0) = 2$$

$$x(0) = 3, y(0) = -4$$

$$23. \begin{cases} x' = 5x + 15y \\ y' = -3x - y \\ x(0) = 1, y(0) = 1 \end{cases}$$

$$24. \begin{cases} x' = 3x + y \\ y' = -4x - y \\ x(0) = 7, y(0) = -1 \end{cases}$$

$$25. \begin{cases} x' = x \\ y' = -5x - 2y \\ x(0) = -1, y(0) = 7 \end{cases}$$

$$26. \begin{cases} x' = x - 2y \\ y' = 2x + 5y \\ x(0) = 2, y(0) = -2 \end{cases}$$

$$27. \begin{cases} x' = 3x + 2y \\ y' = -10x - y \\ x(0) = -1, y(0) = 7 \end{cases}$$

$$28. \begin{cases} x' = -x - y \\ y' = x - y \\ x(0) = 1, y(0) = 0 \end{cases}$$

$$29. \begin{cases} x' = -x + y \\ y' = -y \\ x(0) = 2, y(0) = 1 \end{cases}$$

$$30. \begin{cases} x' = -8y \\ y' = 2x \\ x(0) = 2, y(0) = 0 \end{cases}$$

IV

Найти общее решение системы матричным способом.

$$1. \begin{cases} x' = -3x - y - z \\ y' = 6x + 6y + 5z \\ z' = -x - 3y - 2z \end{cases}$$

$$2. \begin{cases} x' = x + 3y \\ y' = 3x - 2y - z \\ z' = -y + z \end{cases}$$

$$3. \begin{cases} x' = 2x - y - z \\ y' = -y \\ z' = 2y + z \end{cases}$$

$$4. \begin{cases} x' = 3x - 2y + 2z \\ y' = 4x - 3y - 2z \\ z' = x - y + 2z \end{cases}$$

$$5. \begin{cases} x' = -x + 2y + 3z \\ y' = 2x - 3y - 2z \\ z' = -x + 3y + 3z \end{cases}$$

$$6. \begin{cases} x' = 2x - y \\ y' = 4x - 3y - 2z \\ z' = -z \end{cases}$$

$$7. \begin{cases} x' = 2x + y + z \\ y' = -y - 2z \\ z' = y - 4z \end{cases}$$

$$8. \begin{cases} x' = 3x + y + z \\ y' = 2x + 2y + z \\ z' = x + y + 3z \end{cases}$$

$$9. \begin{cases} x' = x - 2y - 2z \\ y' = x + 4y + 2z \\ z' = -x - y + z \end{cases}$$

$$10. \begin{cases} x' = 5x + 2y + 2z \\ y' = 3x + 4y - 3z \\ z' = -2x - 2y + 3z \end{cases}$$

$$11. \begin{cases} x' = 3x - y - z \\ y' = -x + 5y + z \\ z' = -2x + y + 2z \end{cases}$$

$$12. \begin{cases} x' = x + y + z \\ y' = 3x + y + z \\ z' = 3x - 2y + 4z \end{cases}$$

$$13. \begin{cases} x' = 2x + 2y \\ y' = 2x - 2y - z \\ z' = -y + 2z \end{cases}$$

$$15. \begin{cases} x' = -x + y + z \\ y' = x - y + z \\ z' = x + y + z \end{cases}$$

$$17. \begin{cases} x' = 6x + 5y + 6z \\ y' = -3x - 2y - z \\ z' = -x - y - 3z \end{cases}$$

$$19. \begin{cases} x' = 2y - z \\ y' = x + y - z \\ z' = -x + y + z \end{cases}$$

$$21. \begin{cases} x' = x - y \\ y' = -x - 2y + 3z \\ z' = 3y + z \end{cases}$$

$$23. \begin{cases} x' = -3x - 2y + 2z \\ y' = 3x + 3y - z \\ z' = 2x + 3y - z \end{cases}$$

$$25. \begin{cases} x' = x + y + z \\ y' = x - y + z \\ z' = x + y - z \end{cases}$$

$$27. \begin{cases} x' = 4x + 3y - 2z \\ y' = x + y + z \\ z' = x + 3y + z \end{cases}$$

$$29. \begin{cases} x' = -x + 2y + z \\ y' = x + z \\ z' = 4x - 4y + 2z \end{cases}$$

$$14. \begin{cases} x' = x - y + z \\ y' = 2x - 2y + z \\ z' = -5x + 2y + 4z \end{cases}$$

$$16. \begin{cases} x' = x - y + z \\ y' = x + y - z \\ z' = 2x - y \end{cases}$$

$$18. \begin{cases} x' = 3x - y + 3z \\ y' = 3x - y + 2z \\ z' = -2x + 2y - 3z \end{cases}$$

$$20. \begin{cases} x' = 3x - 6y \\ y' = -6x - 3y + 2z \\ z' = 2y + 3z \end{cases}$$

$$22. \begin{cases} x' = 2x + y - z \\ y' = 2x + 3y - 2z \\ z' = -2x + 4y - 3z \end{cases}$$

$$24. \begin{cases} x' = -3x - 2y + 4z \\ y' = -x + 2y + z \\ z' = -2x + 2y + 3z \end{cases}$$

$$26. \begin{cases} x' = 4x - 5y + 2z \\ y' = x + y - z \\ z' = x + 2y - 2z \end{cases}$$

$$28. \begin{cases} x' = -2x + 3y - 2z \\ y' = y - 2z \\ z' = -z \end{cases}$$

$$30. \begin{cases} x' = -y - z \\ y' = x + 2y - z \\ z' = -2x - 2y + z \end{cases}$$